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# Time-dependent Simple Temporal Networks

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*October 10th, 2012*

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## STN (Simple Temporal Networks) [DechterMeiriPearl91]

Framework for managing constraints of the form  $y - x \geq c$ , with  $c$  a constant  
Several problems over STN **solvable in polytime**

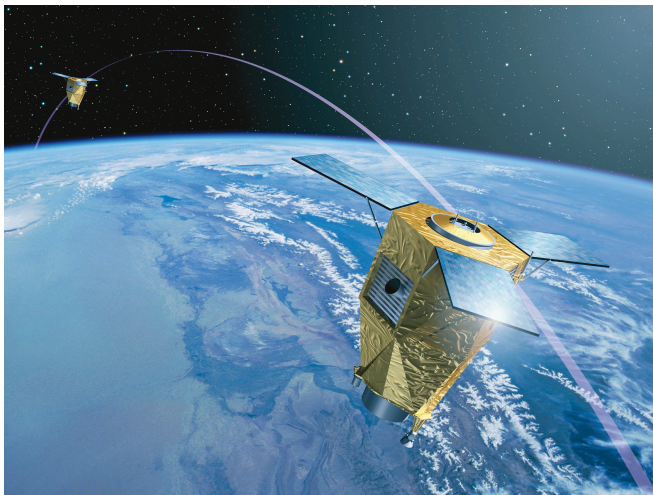
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Paper's contribution: **TSTN (Time-dependent Simple Temporal Networks)**

Framework for managing constraints of the form  $y - x \geq dmin(x, y)$   
(min distance between  $x$  and  $y$  depending on the time at which the transition from  $x$  to  $y$  occurs)

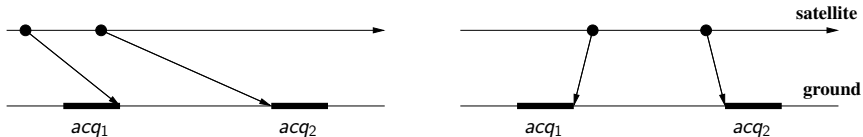
# Motivation: agile satellites



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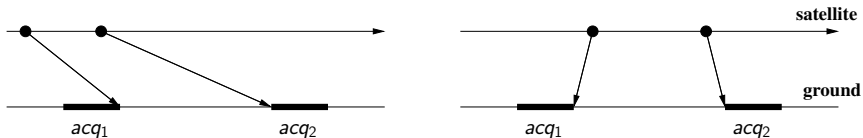
# Motivations for constraints $y - x \geq dmin(x, y)$

## Modeling of **constraints for agile satellites**



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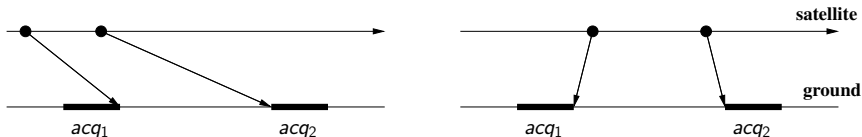
## Modeling of **constraints for agile satellites**



$$sta_2 - end_1 \geq \underbrace{minAttTransTime(EndAtt_1(end_1), StaAtt_2(sta_2))}_{dmin(end_1, sta_2)}$$

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Other problems covered:

- ▶ **time-dependent scheduling:**  $y - x \geq p(x)$   
Example: logistics with traffic congestion
- ▶ **simple temporal problems:**  $y - x \geq c$



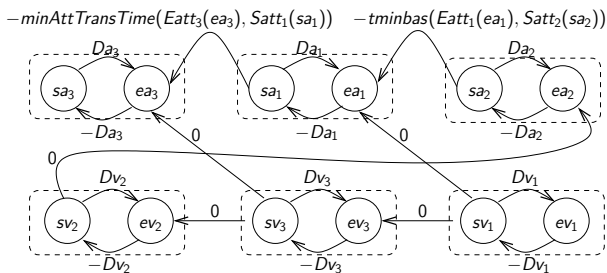
**TSTN (Time-dependent Simple Temporal Network)** = pair  $(V, C)$  with:

- ▶  $V$  finite set of **variables** whose domain is an interval  $[l, u] \subset \mathbb{R}$
- ▶  $C$  finite set of constraints of the form  $c : y - x \geq dmin(x, y)$  with  $dmin : \mathbf{D}(x) \times \mathbf{D}(y) \rightarrow \mathbb{R}$

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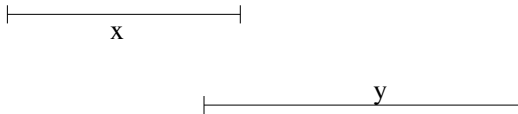
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As in STN, notion of **distance graph** (one arc  $y \rightarrow x$  weighted by  $-dmin(x, y)$  per constraint  $y - x \geq dmin(x, y)$ )



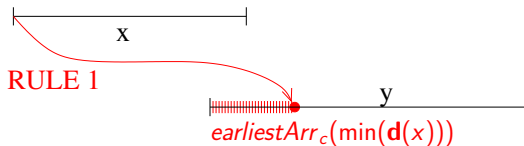
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Propagation rules enforcing **Bound-AC (BAC)**:



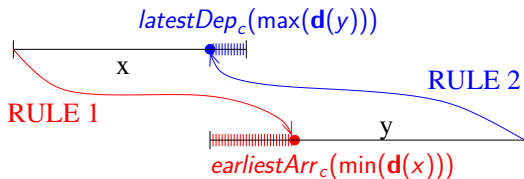
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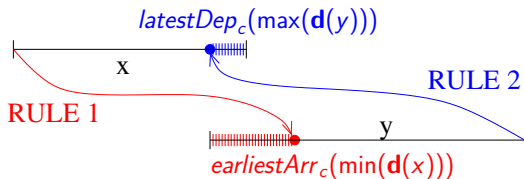
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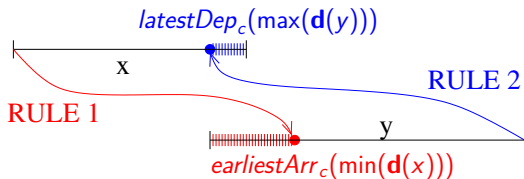
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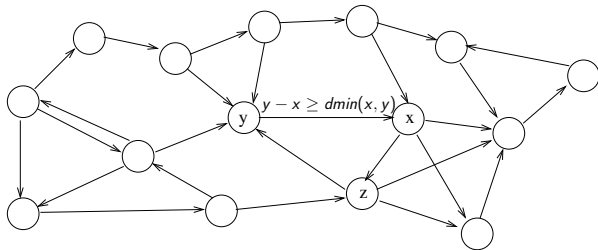
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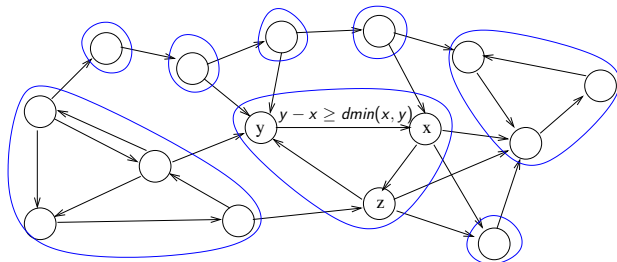


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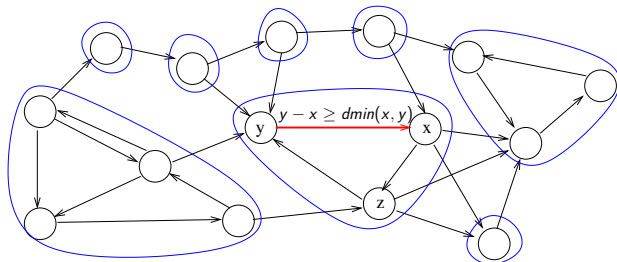
For agile satellites, coupling with a **continuous control optimization library**



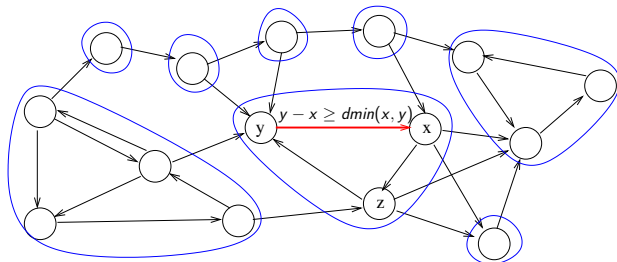




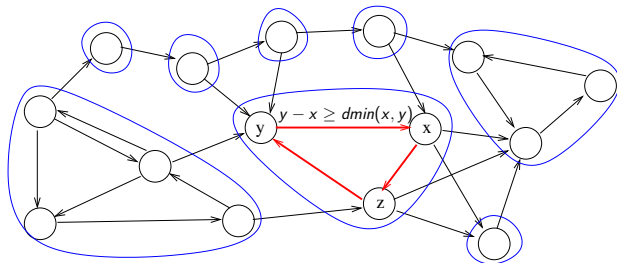
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4. Inconsistency detection based on **propagation cycle detection** (difference with STN: inconsistency  $\leftrightarrow$  existence of a propagation cycle)

Algorithm establishing BAC over TSTN in  $O(|V||C|)$  **constraint revisions**  
**(under some conditions)**

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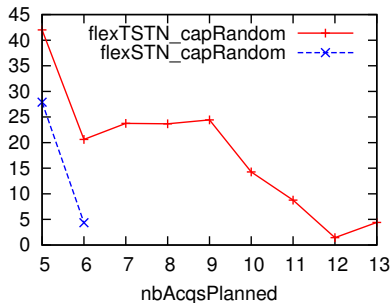
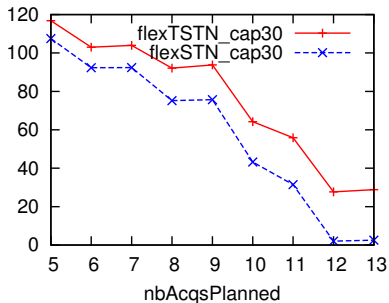
## Prop. 3

Contrarily to STN, even if all constraints are BAC (or AC), values remaining in the domains are **not necessarily globally consistent**

Globally consistency OK **if** delay-monotonicity and only simple temporal constraints ( $dmin(x, y) = c$ ) in cycles of the distance graph



## Practical results on agile satellites



Result: with TSTN, **more acquisitions** and **more flexibility** on acquisition plans than with STN based on constant upper bounds on transition times

TSTN = **temporal layer** of a constraint-based local search solver developed for handling space missions

Other aspects taken into account (not presented here):

- ▶ constraints on **resources** (energy, memory, temperature...)
- ▶ several optimization **criteria**
- ▶ **operational** constraints